

# MUESTREO ALEATORIO SIMPLE (MAS)

Parámetros	Estimadores	Intervalos de confianza (1-α)
M	$\frac{1}{n} \sum y_i = \bar{y} = \bar{u}$	$\bar{y} \pm B_M$
T = NM	$\hat{T} = N\hat{M} = N\bar{y}$	$\hat{T} \pm B_T$
P	$\hat{p} = \bar{y} = \frac{\sum y_i}{N}$	$\hat{p} \pm B_P$
A = NP	$\hat{A} = N\hat{p}$	$\hat{A} \pm B_A$

Var [y] =  $\frac{\sigma^2}{n} \frac{N-n}{N-1}$

Var [y] =  $\frac{s^2}{n} \left(\frac{N-n}{N}\right)$

$s^2 = \frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2$

S = Desviación estandar

$B_M = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\hat{\text{Var}}[y]} & n > 30 \\ t_{\frac{\alpha}{2}, n-1} \sqrt{\hat{\text{Var}}[y]} & n \leq 30 \end{cases}$

$\hat{\text{Var}}[\hat{T}] = N^2 \frac{s^2}{n} \left(\frac{N-n}{N}\right)$

$B_T = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\hat{\text{Var}}[\hat{T}]} \\ t_{\frac{\alpha}{2}, n-1} \sqrt{\hat{\text{Var}}[\hat{T}]} \end{cases}$

$\hat{T} \pm B_T = N(\bar{y} \pm B_M)$

$\hat{\text{Var}}[\hat{p}] = \frac{\hat{p}(1-\hat{p})}{n-1} \left(\frac{N-n}{N}\right)$

$B_P = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\hat{\text{Var}}[\hat{p}]} & n \geq 100 \\ t_{\frac{\alpha}{2}, n-1} \sqrt{\hat{\text{Var}}[\hat{p}]} & n < 100 \end{cases}$

$\hat{\text{Var}}[\hat{A}] = N^2 \frac{\hat{p}(1-\hat{p})}{n-1} \left(\frac{N-n}{N}\right)$

$B_A = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\hat{\text{Var}}[\hat{A}]} \\ t_{\frac{\alpha}{2}, n-1} \sqrt{\hat{\text{Var}}[\hat{A}]} \end{cases}$

$\hat{A} \pm B_A = N(\hat{p} \pm B_P)$

### TAMAÑO DE MUESTRA MAS

$$n = \frac{\sigma^2 N}{(N-1) \frac{B^2}{z_{\alpha/2}^2} + \sigma^2} \quad (\text{Promedio})$$

En proporciones lo unico que cambia es que

$$\sigma^2 = P(1-P)$$

Por lo que

$$n = \frac{1}{\frac{1}{N} + \frac{N-1}{N} \cdot \frac{1}{n_0}}$$

$$n = \frac{P(1-P) N}{(N-1) \frac{B^2}{z_{\alpha/2}^2} + P(1-P)} \quad (\text{Propedio})$$

$$n_0 = \frac{z_{\alpha/2}^2 \cdot \sigma^2}{B^2} \rightarrow \text{Tamaño de muestra para poblaciones infinitas}$$

$$n = \frac{P(1-P)}{(N-1) \frac{B^2}{z_{\alpha/2}^2 \cdot N^2} + P(1-P)} \quad (\text{Total})$$

$$n = \frac{N \sigma^2}{(N-1) \frac{B^2}{z_{\alpha/2}^2 \cdot N^2} + \sigma^2} \quad (\text{Total})$$

### MUESTREO ALEATORIO ESTRATIFICADO (MAE)

Parámetros	Estimadores	Intervalo de confianza
$N$	$\sum_{i=1}^L N_i$	---
$n$	$\sum_{i=1}^L n_i$	---
$\hat{\bar{Y}}_{st}$	$\hat{\bar{Y}}_{st} = \sum_{i=1}^L \hat{Y}_i = \sum_{i=1}^L N_i \bar{y}_i$	$\hat{\bar{Y}}_{st} \pm B_{\hat{\bar{Y}}_{st}}$
$M_{st}$	$\bar{Y}_{st} = \frac{1}{N} \sum_{i=1}^L N_i \bar{y}_i = \frac{\hat{\bar{Y}}_{st}}{N}$	$\bar{Y}_{st} \pm B_{M_{st}}$
$A_{st}$	$\hat{A}_{st} = \sum_{i=1}^L N_i \hat{P}_i = \sum_{i=1}^L \hat{A}_i$	$\hat{A}_{st} \pm B_{\hat{A}_{st}}$
$P_{st}$	$\hat{P}_{st} = \frac{1}{N} \sum_{i=1}^L N_i \hat{P}_i = \frac{\hat{A}_{st}}{N}$	$\hat{P}_{st} \pm B_{\hat{P}_{st}}$

$$\begin{aligned} \text{Var}[\hat{\bar{Y}}_{st}] &= \sum_{i=1}^L N_i^2 \cdot \text{Var}[\bar{y}_i] \\ &= \sum_{i=1}^L N_i^2 \frac{S_i^2}{n_i} \left( \frac{N_i - n_i}{N_i} \right) \end{aligned}$$

$$\begin{aligned} \text{Var}[\hat{A}_{st}] &= \sum_{i=1}^L N_i^2 \cdot \text{Var}[\hat{P}_i] \\ &= \sum_{i=1}^L N_i^2 \frac{\hat{P}_i (1 - \hat{P}_i)}{n_i - 1} \left( \frac{N_i - n_i}{N_i} \right) \end{aligned}$$

$$B_{Est} = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot s_i^2}{n_i} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n > 30 \\ t_{\frac{\alpha}{2}, n-L} \sqrt{\sum_{i=1}^L \frac{N_i \cdot s_i^2}{n_i} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n \leq 30 \end{cases} \quad \left| \quad B_{Est} = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot \hat{p}_i(1-\hat{p}_i)}{n_i-1} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n > 30 \\ t_{\frac{\alpha}{2}, n-L} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot \hat{p}_i(1-\hat{p}_i)}{n_i-1} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n \leq 30 \end{cases}$$

$$\begin{aligned} \text{Var}[\hat{y}_{Est}] &= \frac{1}{N^2} \cdot \text{Var}[\hat{t}_{Est}] \\ &= \sum_{i=1}^L \frac{N_i^2}{N^2} \cdot \frac{s_i^2}{n_i} \cdot \left(\frac{N_i - n_i}{N_i}\right) \end{aligned}$$

$$\begin{aligned} \text{Var}[\hat{p}_{Est}] &= \frac{1}{N^2} \cdot \text{Var}[\hat{A}_{Est}] \\ &= \sum_{i=1}^L \frac{N_i^2}{N^2} \cdot \frac{\hat{p}_i(1-\hat{p}_i)}{n_i-1} \cdot \left(\frac{N_i - n_i}{N_i}\right) \end{aligned}$$

$$B_{M_{Est}} = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot s_i^2}{N^2} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n > 30 \\ t_{\frac{\alpha}{2}, n-L} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot s_i^2}{N^2} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n \leq 30 \end{cases} \quad \left| \quad B_{P_{Est}} = \begin{cases} z_{\frac{\alpha}{2}} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot \hat{p}_i(1-\hat{p}_i)}{N^2} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n > 30 \\ t_{\frac{\alpha}{2}, n-L} \sqrt{\sum_{i=1}^L \frac{N_i^2 \cdot \hat{p}_i(1-\hat{p}_i)}{N^2} \cdot \left(\frac{N_i - n_i}{N_i}\right)} & n \leq 30 \end{cases}$$

$$\bar{y} \pm B_M = \frac{1}{N} (\hat{t}_{Est} \pm B_{t_{Est}})$$

$$\hat{p} \pm B_{P_{Est}} = \frac{1}{N} (\hat{A}_{Est} \pm B_{A_{Est}})$$

### TAMAÑO DE MUESTRA MAE

$$n = \frac{\sum_{i=1}^L N_i^2 \cdot \sigma_i^2 / w_i}{DN^2 + \sum_{i=1}^L N_i \sigma_i^2}; \quad D = \frac{B^2}{z_{\frac{\alpha}{2}}^2}$$

Donde  $w_i$  depende de la asignación

• Para  $M$   
 $\sigma^2 = s^2$   
 $\sigma = (y_{i\max} - y_{i\min})/6$

• Para  $P$   
 $\sigma^2 = \hat{p}(1-\hat{p})$

• Para totales el cambio es en  $D$

$$D = \frac{B^2}{z_{\frac{\alpha}{2}}^2 \cdot N^2}$$

- Asignación Óptima con Costos Variables

$C_i = \text{diferentes}$ ;  $\sigma_i = \text{diferentes}$   
 $w_i \propto \sigma_i$ ;  $w_i \propto 1/\sqrt{c_i}$ ;  $w_i \propto N_i$

$$C = C_0 + \sum_{i=1}^L C_i n_i$$

$$w_i = \frac{N_i \cdot \sigma_i / \sqrt{c_i}}{\sum_{k=1}^L N_k \cdot \sigma_k / \sqrt{c_k}}$$

- Asignación de Neyman

$C_1 = C_2 = C_3 = \dots = C_n$ ;  $\sigma_i = \text{diferentes}$

$$w_i = \frac{N_i \cdot \sigma_i}{\sum_{k=1}^L N_k \cdot \sigma_k}$$

- Asignación Proporcional

$C_1 = C_2 = C_3 = \dots = C_n$ ;  $\sigma_i = \text{Iguales}$

$$w_i = \frac{N_i}{N}$$